

(in the manner described hereinbelow) which transform the Z cell edges ZA, ZB and ZC into the Y cell edges YA, YB and YC, respectively, within the respective specified tolerance values TOL11, TOL12 and TOL13.

Next, the number of matrix triples determined in step 30 is tested in steps 40a and 40b to determine whether no matrix triples were found (step 40a) or a number of matrix triples were found exceeding a predetermined limit (e.g. 2000) (step 40b). If no matrix triples were found, further computations are terminated and a new cell Y is selected for comparison with cell Z in step 50a (when the identity of the lattice structure corresponding to cell Z is being sought). If too many matrix triples are found, further computations are terminated and an error signal is produced in step 50b.

If at least one set, but not an excessive number, of matrix triples are found in step 30, then all combinations of those matrix triples found in step 30 are determined in step 60 (in the manner described hereinbelow) which also transform the Z cell angles ZAL, ZBE and ZGA into the Y cell angles YAL, YBE and YGA, respectively, within the respective specified tolerance values TOL14, TOL15 and TOL16. Each combination of matrix triples found is saved as the elements U1, V1, W1, U2, V2, W2, U3, V3, W3 of a transformation matrix H.

The actual tolerances TOLA, TOLB, TOLC, TOLAL, TOLBE, TOLGA for each transformation matrix H determined in step 60 are calculated in step 70, and the inverse H' of each matrix H is calculated in step 80.

Referring to FIG. 3, a preferred method for determining the matrix triples in step 30 will now be described. First, in step 301, a set of a predetermined number NHEL of possible integer and rational number values HEL(JJ), HEL(KK), HEL(LL) (JJ, KK, LL = 1, 2, . . . NHEL) for the elements of a transformation matrix H are defined (stored). A typical range of values HEL is $-6 \leq \text{HEL} \leq 6$, including both the integer values $\pm 1, \pm 2, \pm 3, \pm 4, \pm 5, \pm 6$, and the non-integer rational number inverses thereof, i.e., $\pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{1}{4}, \pm \frac{1}{5}$ and $\pm \frac{1}{6}$. The range of values HEL is normally selected based on the type of problem to be solved. With reduced versions of cells Y and Z, for example, the range of potential values for values HEL is reduced. In addition, variable indices ICTMA, ICTMB and ICTMC, which are respectively used to identify the matrix triples AU, AV, AW; BU, BV, BW; and CU, CV, CW determined to transform the respective Z-cell edges into the corresponding Y-cell edges within the respective specified tolerances, as described hereinabove, are initialized to zero.

In steps 302-310, variable indices JJ, KK and LL for signifying individual ones of the values HEL and controlling iteration of computation loops are initialized, incremented and compared with NHEL in the sequence shown to provide first, second and third nested computation loops using successive combinations of HEL(JJ), HEL(KK) and HEL(LL) as described in more detail hereinbelow.

Since JJ, KK, and LL initially are not greater than NHEL, as determined in steps 304, 307 and 310, respectively, a symmetrical dot product TZEE for transformed cell Z is calculated in step 312 using values HEL(JJ), HEL(KK) and HEL(LL) and dot products Z11, Z22, Z33, Z23, Z13 and Z12 for cell Z calculated in step 20 (FIG. 2) as follows:

$$\begin{aligned} TZEE = & \text{HEL}(JJ) \cdot \text{HEL}(JJ) \cdot Z11 + \text{HEL}(KK) \cdot \text{HEL}(KK) \cdot Z22 + \\ & \text{HEL}(LL) \cdot \text{HEL}(LL) \cdot Z33 + 2.0 (\text{HEL}(KK) \cdot \text{HEL}(LL) \cdot Z23 + \\ & \text{HEL}(JJ) \cdot \text{HEL}(LL) \cdot Z13 + \text{HEL}(JJ) \cdot \text{HEL}(KK) \cdot Z12) \end{aligned}$$

It will be appreciated that the values HEL(JJ), HEL(KK) and HEL(LL) form a row of a transformation matrix and that the calculated dot product may correspond to A.A, B.B or C.C depending on the order of the matrix row in the final transformation matrix H.

Next, in step 314, dot product TZEE is tested to determine whether it is greater than zero. If not, no further computations are done using the current combination of values HEL, and the third computation loop comprising steps 309-346 is restarted using a new value of HEL(LL) by returning to step 309.

If $TZEE > 0$, then a transformed edge for cell Z, TZEDG, is derived (step 316) as follows:

$$TZEDG = \sqrt{TZEE}$$

Then TZEDG is tested (step 318) to determine whether it constitutes a transformation of Z-cell edge ZA to Y-cell edge YA within the specified tolerance TOL11 by determining whether:

$$(TOL11 - |TZEDG - YA|) < 0.$$

If the determination in step 318 is TRUE (i.e., the foregoing inequality is FALSE) then the current values of HEL(JJ), HEL(KK) and HEL(LL) from which TZEDG was derived is a possible row in a transformation matrix H; and the counter ICTMA is thus incremented (step 320), and the values HEL(JJ), HEL(KK) and HEL(LL) are saved (step 322) as matrix triple AU(ICTMA), AV(ICTMA) and AW(ICTMA), respectively. A value DA(ICTMA) = TZEDG - YA representing the actual tolerance (difference) between the transformed Z cell edge A and the inputted Y-cell YA is also calculated and saved (step 324); together with a value TZA(ICTMA) = TZEDG as the transformed Z-cell edge a parameter (step 326). The computation then proceeds to step 328.

If a FALSE determination is made in step 318 (i.e., the inequality is TRUE), then TZEDG is similarly tested in step 328 to determine whether it constitutes a transformation of the Z-cell edge ZB to the Y-cell edge YB within the specified tolerance TOL12, i.e., whether $(TOL12 - |TZEDG - YB|) < 0$. Similarly to steps 320-326, if the determination in step 328 is TRUE, then the counter ICTMB is incremented (step 330); the current values of HEL(JJ), HEL(KK) and HEL(LL) are saved (step 332) as matrix triple BU(ICTMB), BV(ICTMB), BW(ICTMB); values DB(ICTMB) = TZEDG - YB, and TZB(ICTMB) = TZEDG are calculated and saved (steps 334-336); and the computation proceeds to step 338.

If a FALSE determination is made in step 328, then TZEDG is again similarly tested in step 338 with respect to Y-cell edge YC to determine whether $(TOL13 - |TZEDG - YC|) < 0$. Similarly to steps 320-326 and 330-336, if the determination in step 338 is TRUE, then counter ICTMC is incremented (step 340); the current values of HEL(JJ), HEL(KK) and HEL(LL) are saved (step 342) as matrix triple CU(ICTMC), CV(ICTMC),